

THE COMPLETE THEORY OF MATHEMATICS

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ABSTRACT. This study focuses on the functional framework $x(z) = \lambda z^\mu$ for a non-linear PDE arising from a fluid in a sphere.

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1. INTRODUCTION

During the past few decades, research in flows involving heat transfer of non-Newtonian fluids has been intensified.

2. PRELIMINARY

We define some basic results from Kim [1] for the benefit of all.

Definition 1: A solution $u \in \Omega$ is called a α -weak solution of the boundary value problem ...

3. THE HEART OF THE MATTER

The heart of the matter is to state without proof the following:

Lemma 1: (A Sobolev's embedding) Let $u \in \Omega$. Then we have the estimate

$$\int r^m u' v' dr + (a - m) \int r^{m-1} u' v dr = \int r^m [h - g(u)] v dr, \quad (1)$$

Next we proof the main theorem:

Theorem 1: (A priori estimates). Let u be a solution of ...

Proof: We split the proof into two steps.

The solution to equation (1) is investigated numerically and ...

Table 1. Comparison of perturbation and numerical result with $\Lambda = \Gamma = 1$ and $\delta = 0.2$.

γ	θ_{max} (PS)	θ_{max} (NS)	Rel. error
0	0.6439	0.6635	1.94%
1	0.6458	0.6684	2.39%
2	0.6476	0.6737	3.87%
4	0.6513	0.6846	4.87%
5	0.6531	0.6904	5.40%

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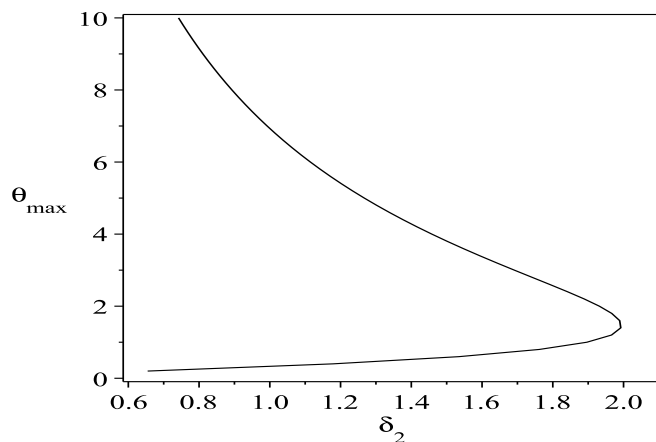


Fig. 1. Bifurcation plot for a variable viscosity when $\Gamma = \Lambda = 1$.

4. CONCLUDING REMARKS

Functional framework (see Evans and Alli [2]) has been employed to generate analytical solutions of a model reaction diffusion equation. Table 1 demonstrates the comparison of solutions.

In Fig. 1, the critical value of the temperature is plotted against Newtonian parameter δ .

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NOMENCLATURE

$\theta_{max\ cr}$ Non-dimensionless temperature of the model
 ϵ Activation Energy

REFERENCES

- [1] S. O. Kim, *Thermal stability of a reactive non-Newtonian flow in a sphere*, Int. Commu. Heat and Mass Transfer **60** (1) 70-81, 2009.
- [2] L. C. Evans and P. A. Alli, *Partial Differential Equations*, American Mathematical Society, Providence, Rhode Island, 1998.
- [3] H. A. Okoye, *How to define reasonably weighted Sobolev spaces*, Ph.D. thesis, University of Uyo, Uyo, Akwa Ibom State, Nigeria, 2009.

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